

today:

midterm: 5.1 - 5.6, 6.1

homework 2 due (5.5.36, 5.5.74, 5.6.4, 5.review.38, 6.1.32, 6.1.48)

§ 6.2 - volumes

thursday:

§ 6.3 - volumes by cylindrical shells

(special guest lecturer Jim)

tuesday:

§ 6.4 - applications

quiz: 6.1 - 6.2

wednesday, 21 october:

webwork 3 due

thursday, 22 october:

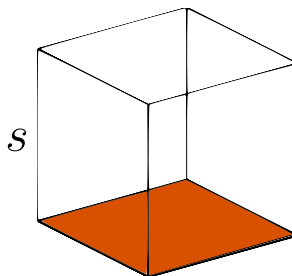
§ 7.1 - integration by parts

§ 7.2 - trigonometric integrals

homework 3 due (§ 6.2, § 6.3)

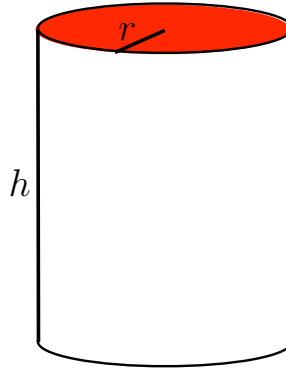
example i

- what is the volume of a cube with sides of length s ?
- volume = s^3
- base area = s^2
- vol = (base area)(height)



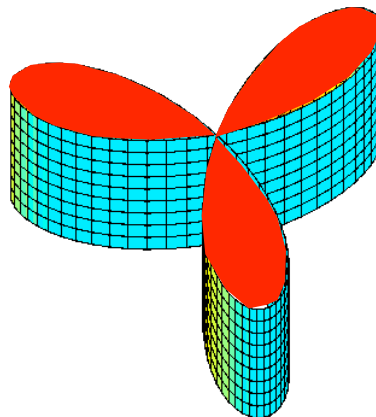
example ii

- what is the volume of a cylinder with radius r and height h ?
- volume = $\pi r^2 h$
- base area = πr^2
- vol = (base area)(height)



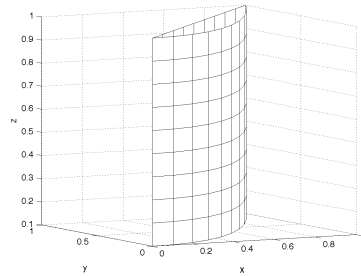
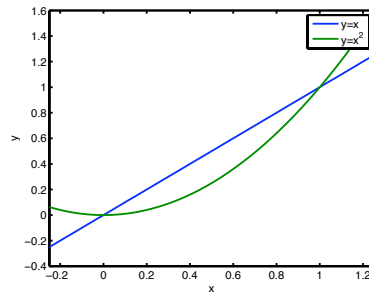
fact

- a shape with uniform cross sections is called a **generalized cylinder**
- the volume of a generalized cylinder is the cross-sectional area times the height



example iii

- Find the volume of the generalized cylinder of height 1 with base bounded by $y = x^2$ and $y = x$.



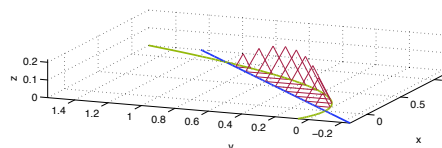
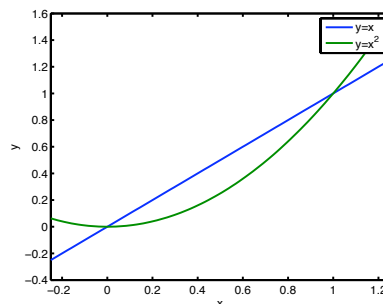
Note: This is not a generalized cylinder. The triangular prisms of width dx are, however.

example iv

height of an equilateral triangle is $\sqrt{3}/2$ times the base (think 30-60-90 triangle)

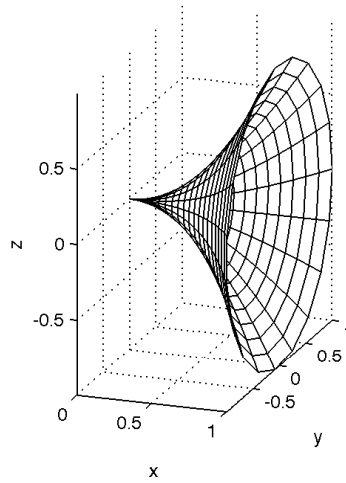
can also use semi-circles, squares, etc...

- Suppose the base of a figure is bounded by the curves $y = x^2$ and $y = x$.
- Suppose further that cross-sections parallel to the y axis and perpendicular to the x y plane are equilateral triangles.
- Find the volume of the figure.



example v

- Consider the solid generated by rotating the area under the curve $y = x^2$ between $x = 0$ and $x = 1$ about the x axis.
- What is this solid's volume?
- Note: The cross sections are circular.



next time

- read § 6.3